



# Robot Programming with Lisp 6. Search Algorithms

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November 22<sup>nd</sup>, 2018





#### **Contents** Problem Definition

 $\Delta *$ Hill-climbing aka gradient ascent/descent

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#### Deterministic, fully observable $\implies$ single-state problem

Agent knows exactly which state it will be in.

Solution is a sequence of actions

#### $\textbf{Deterministic, non-observable} \Longrightarrow \textit{conformant problem}$

Agent may have no idea where it is.

Solution (if any) is a sequence of actions

Nondeterministic, partially observable  $\Longrightarrow$  contingency problem

must perceive the world during execution

solution is a contingent plan or a policy

often replan during execution

**Unknown state space**  $\implies$  *exploration problem* ("online")

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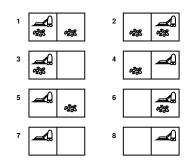


# Example: vacuum world

**Single-state**, start in #5. **Solution**? [Right, Vacuum]

**Conformant**, start in  $\{1, 2, 3, 4, 5, 6, 7, 8\}$ e.g., *Right* goes to  $\{2, 4, 6, 8\}$ . **Solution**? [Right, Vacuum, Left, Vacuum]

**Contingency**, start in #5 *Vacuum* can dirty a clean carpet. Local sensing only at current location. **Solution**? [Right, if dirt then Vacuum]



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# Single-state problem formulation

A *problem* is defined by four items:

- initial state
- operators (or successor function S(x))
   e.g., Vacuum(x) → clean room
- goal test
- *path cost* (additive)
  - e.g., sum of distances, number of operators executed, etc.

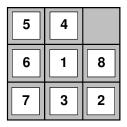
A  $\mathit{solution}$  is a sequence of operators leading from the initial state to a goal state

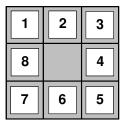






# Example: The 8-puzzle





Start State

**Goal State** 

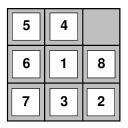
states ? operators ? goal test ? path cost ?

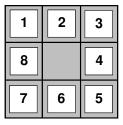
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# Example: The 8-puzzle





Start State

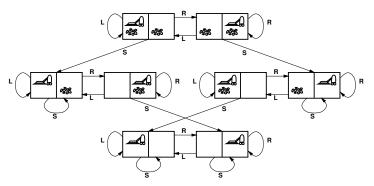
**Goal State** 

states: integer locations of tiles (ignore intermediate positions)
operators: move blank left, right, up, down (ignore unjamming etc.)
goal test: current state = goal state
path cost: 1 per move





## Example: vacuum world state space graph



#### states ? operators ? goal test ? path cost ?

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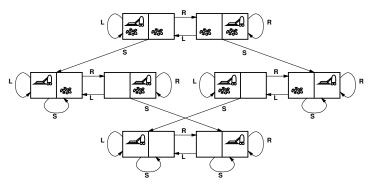
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## Example: vacuum world state space graph



states: integer dirt and robot locations (ignore dirt amounts)
operators: Left, Right, Vacuum
goal test: no dirt in current state
path cost: 1 per operator

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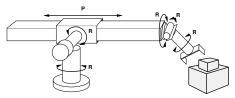
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# Example: robotic assembly

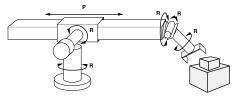


#### states ? operators ? goal test ? path cost ?

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# Example: robotic assembly



states: real-valued coordinates of robot joint angles and parts of the
object to be assembled
operators: continuous motions of robot joints
goal test: assembly object is complete
path cost: time to execute







# Search algorithms

Basic idea:

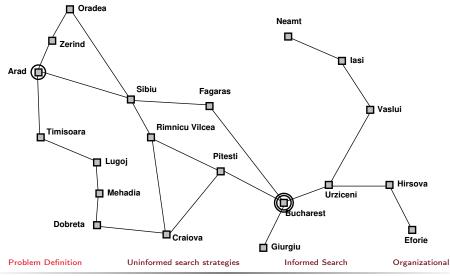
offline, simulated exploration of state space by generating successors of already-explored states (a.k.a. *expanding* states)

function General-Search( problem, strategy) returns a solution, or failure
initialize the search tree using the initial state of problem
loop do
 if there are no candidates for expansion then return failure
 choose a leaf node for expansion according to strategy
 if the node contains a goal state then return corresponding solution
 else expand the node and add the resulting nodes to the search tree
end





## General search example



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# General search example



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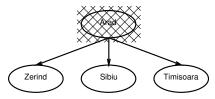
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### General search example



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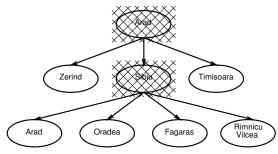
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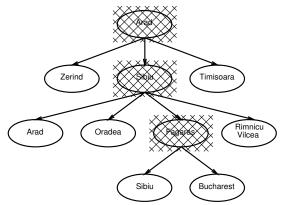
### General search example







### General search example









# Implementation of search algorithms

```
 \begin{array}{l} \mbox{function General-Search(problem, Queuing-Fn) returns a solution, or failure} \\ nodes \leftarrow Make-Queue(Make-Node(Initial-State[problem])) \\ \mbox{loop do} \\ \mbox{if nodes is empty then return failure} \\ node \leftarrow Remove-Front(nodes) \\ \mbox{if Goal-Test[problem] applied to State(node) succeeds then return} \\ node \\ nodes \leftarrow Queuing-Fn(nodes, Expand(node, Operators[problem])) \\ \mbox{end} \end{array}
```

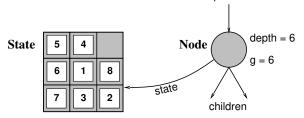






## Implementation contd: states vs. nodes

A *state* is a (representation of) a physical configuration A *node* is a data structure constituting part of a search tree includes *parent*, *children*, *depth*, *path cost* g(x)*States* do not have parents, children, depth, or path cost!



The Expand function creates new nodes, filling in the various fields and using the Operators (or SuccessorFn) of the problem to create the corresponding states.

parent

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# Search strategies

A strategy is defined by picking the *order of node expansion* Strategies are evaluated along the following dimensions:

- completeness—does it always find a solution if one exists?
- time complexity—number of nodes generated/expanded
- space complexity-maximum number of nodes in memory
- optimality—does it always find a least-cost solution?

Time and space complexity are measured in terms of

- b maximum branching factor of the search tree
- d depth of the least-cost solution
- m maximum depth of the state space (may be  $\infty$ )

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# Uninformed search strategies

Uninformed strategies use only the information available in the problem definition Uninformed search strategies are:

- Breadth-first search
- Uniform-cost search
- Depth-first search
- Depth-limited search
- Iterative deepening search

#### **Problem Definition**

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# Breadth-first search

Expand shallowest unexpanded node

#### Implementation:

QueueingFn = put successors at end of queue (FIFO queue)



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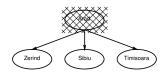
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# Breadth-first search



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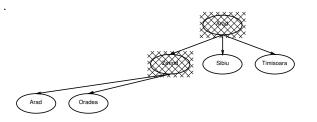
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# Breadth-first search

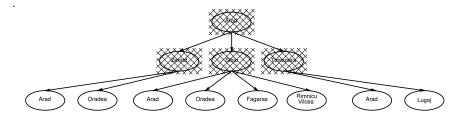








# Breadth-first search









# Properties of breadth-first search

Complete ? Time ? Space ? Optimal ?

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# Properties of breadth-first search

**Complete**: Yes **Time**:  $1 + b + b^2 + b^3 + ... + b^d = O(b^d)$ , i.e., exponential in *d*  **Space**:  $O(b^d)$  (keeps every node in memory) **Optimal**: Yes (if cost = 1 per step); not optimal in general

Space is the big problem; can easily generate nodes at N MB/sec.

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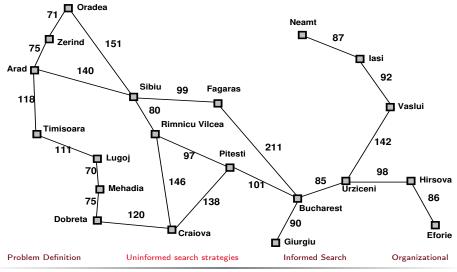
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# Romania with step costs in km



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# Uniform-cost search

Expand least-cost unexpanded node

#### Implementation:

QueueingFn = insert in order of increasing path cost (FIFO queue)



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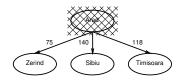
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# Uniform-cost search



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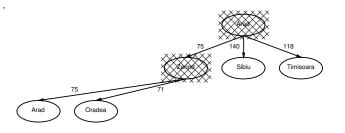
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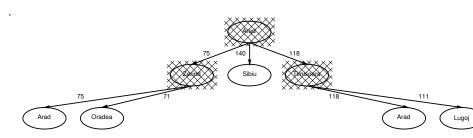
# Uniform-cost search

















# Properties of uniform-cost search

Complete ? Time ? Space ? Optimal ?

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# Properties of uniform-cost search

**Complete**: Yes, if step  $\cot \ge \epsilon$ **Time**: # of nodes with  $g \le \cot \theta$  optimal solution **Space**: # of nodes with  $g \le \cot \theta$  optimal solution **Optimal**: Yes

g(n) is the cost of the path up to node n.



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# Depth-first search

Expand deepest unexpanded node

#### Implementation:

QueueingFn = insert successors at front of queue (LIFO)



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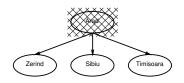
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## Depth-first search

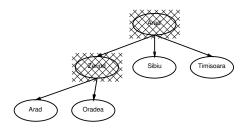








#### Depth-first search

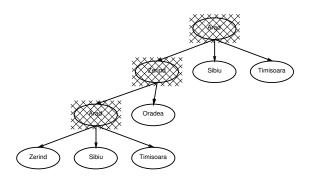








# Depth-first search



I.e., depth-first search can perform infinite cyclic excursions. Need a finite, non-cyclic search space (or repeated-state checking).

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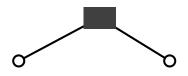
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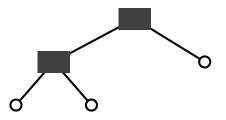
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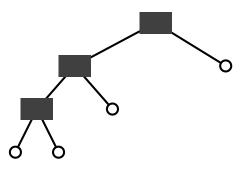
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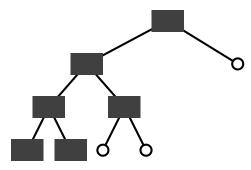
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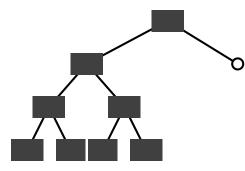
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### DFS on a depth-3 binary tree, contd.



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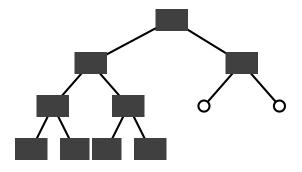
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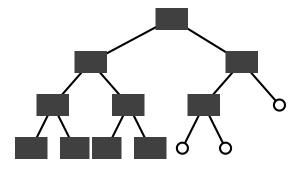
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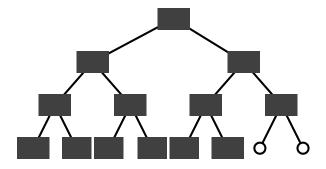
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#### Properties of depth-first search

Complete ? Time ? Space ? Optimal ?

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#### Properties of depth-first search

Complete: No: fails in infinite-depth spaces, spaces with loops  $\Rightarrow$  modify to avoid repeated states along path. Complete in finite spaces Time:  $O(b^m)$ : terrible if *m* is much larger than *d* but if solutions are dense, may be much faster than breadth-first Space: O(bm), i.e., linear space! Optimal: No

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# Depth-limited search

#### Depth-limited search = depth-first search with depth limit I

#### Implementation: Nodes at depth / have no successors

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<pre>function lterative-Deepening-Search( problem) returns a solution sequence inputs: problem, a problem</pre>	
<pre>for depth ← 0 to ∞ do     result ← Depth-Limited-Search( problem, depth)     if result ≠ cutoff then return result end</pre>	



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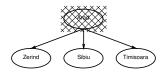
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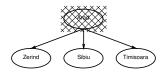
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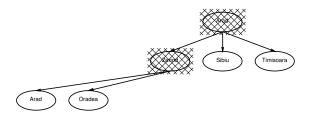
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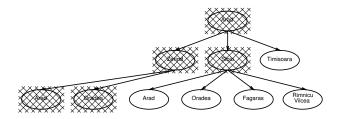








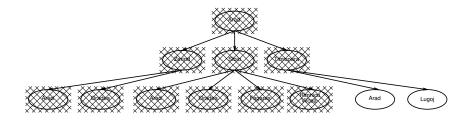












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#### Properties of iterative deepening search

Complete ? Time ? Space ? Optimal ?

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#### Properties of iterative deepening search

Complete: Yes Time:  $(d+1)b^0 + db^1 + (d-1)b^2 + \ldots + b^d = O(b^d)$ Space: O(bd)Optimal: Yes, if step cost = 1

Can be modified to explore uniform-cost tree.

Iterative deepening search uses only linear space and not much more time than other uninformed algorithms







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Greedy Δ\* Heuristics Hill-climbing aka gradient ascent/descent Simulated annealing

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# Idea: use an *evaluation function* for each node as an estimate of "desirability"

 $\Rightarrow$  Expand most desirable unexpanded node

#### Implementation:

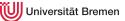
 $\label{eq:QueueingFn} {\sf QueueingFn} = {\sf insert \ successors \ in \ decreasing \ order \ of \ desirability}$ 

Informed search algorithms are:

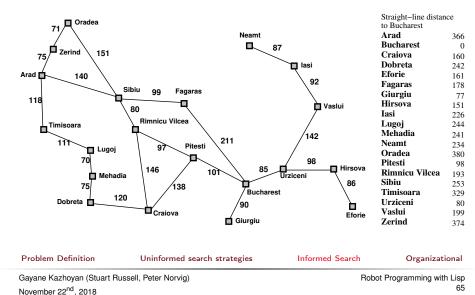
- greedy search
- A\* search

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#### Romania with straight line distances in km







#### Evaluation function h(n) (heuristic) = estimate of cost from *n* to goal

E.g.,  $h_{SLD}(n) = \text{straight-line distance from } n$  to Bucharest

Greedy search expands the node that appears to be closest to goal



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#### Greedy search example



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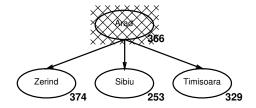
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#### Greedy search example [2]

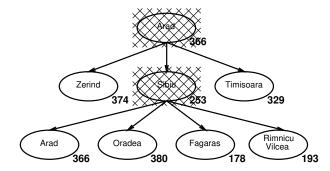








#### Greedy search example [3]

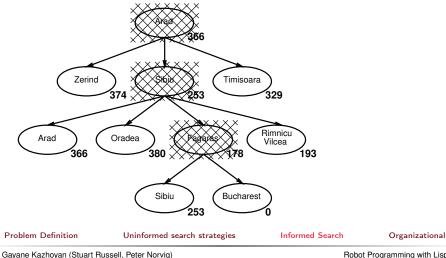








#### Greedy search example [4]



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#### Properties of greedy search

Complete ? Time ? Space ? Optimal ?

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#### Properties of greedy search

Complete: No - can get stuck in loops, e.g.,

 $\mathsf{lasi} \to \mathsf{Neamt} \to \mathsf{lasi} \to \mathsf{Neamt} \to \dots$ 

Complete in finite space with repeated-state checking.

**Time**:  $O(b^m)$ , but a good heuristic can give dramatic improvement **Space**:  $O(b^m)$  — keeps all nodes in memory **Optimal**: No

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### $A^*$ search

Idea: avoid expanding paths that are already expensive

Evaluation function f(n) = g(n) + h(n)

g(n) = cost so far to reach nh(n) = estimated cost to goal from nf(n) = estimated total cost of path through n to goal

A<sup>\*</sup> search uses an *admissible* heuristic i.e.,  $h(n) \le h^*(n)$  where  $h^*(n)$  is the *true* cost from *n*.

E.g.,  $h_{\mathrm{SLD}}(n)$  never overestimates the actual road distance

### Theorem: A\* search is optimal

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### A<sup>\*</sup> search example



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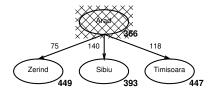
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### A<sup>\*</sup> search example [2]



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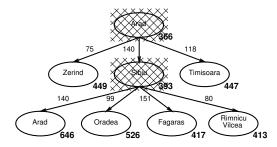
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### $A^{\overline{*}}$ search example [3]

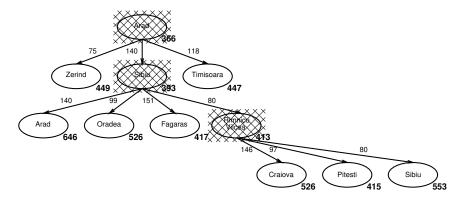








### A<sup>\*</sup> search example [4]

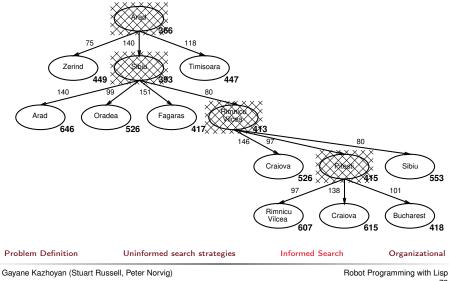








### A<sup>\*</sup> search example [5]

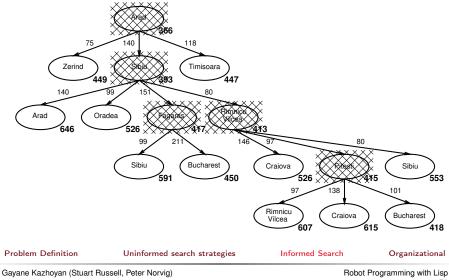


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### A<sup>\*</sup> search example [6]



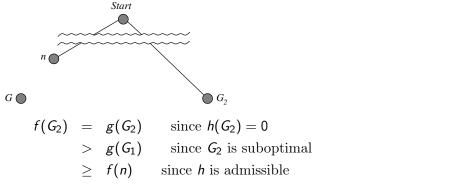
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### Optimality of A<sup>\*</sup> (standard proof)

Suppose some suboptimal goal  $G_2$  has been generated and is in the queue. Let *n* be an unexpanded node on a shortest path to an optimal goal  $G_1$ .



### Since $f(G_2) > f(n)$ , A<sup>\*</sup> will never select $G_2$ for expansion

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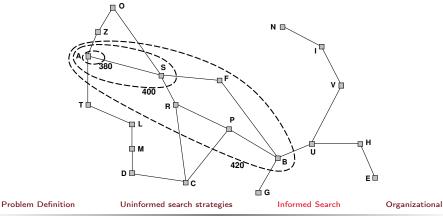
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### Optimality of A<sup>\*</sup> (more useful)

**Lemma**: A\* expands nodes in order of increasing f value Gradually adds "f-contours" of nodes (cf. breadth-first adds layers) Contour i has all nodes with  $f = f_i$ , where  $f_i < f_{i+1}$ 



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### Properties of A\*

Complete ? Time ? Space ? Optimal ?

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**Complete**: Yes, unless there are infinitely many nodes with  $f \le f(G)$ **Time**: Exponential in [relative error in  $h \times$  length of soln.] **Space**: Keeps all nodes in memory **Optimal**: Yes — cannot expand  $f_{i+1}$  until  $f_i$  is finished

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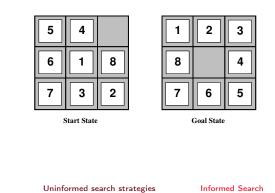
 $h_1(S) = ?$  $h_2(S) = ?$ Problem Definition Universität Bremen

### Admissible heuristics

E.g., for the 8-puzzle:

- $h_1(n) =$  number of misplaced tiles
- $h_2(n) =$ total Manhattan distance

(i.e., no. of squares from desired location of each tile)



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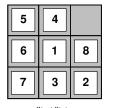
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### Admissible heuristics

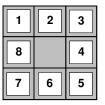
E.g., for the 8-puzzle:

- $h_1(n) =$  number of misplaced tiles
- $h_2(n) =$ total Manhattan distance

(i.e., no. of squares from desired location of each tile)



Start State



Goal State



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If  $h_2(n) \ge h_1(n)$  for all n (both admissible) then  $h_2$  dominates  $h_1$  and is better for search

Typical search costs:

 $d = 14 \quad IDS = 3,473,941 \text{ nodes} \\ A^*(h_1) = 539 \text{ nodes} \\ A^*(h_2) = 113 \text{ nodes} \\ d = 14 \quad IDS = \text{too many nodes} \\ A^*(h_1) = 39,135 \text{ nodes} \\ A^*(h_2) = 1,641 \text{ nodes} \end{cases}$ 

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Admissible heuristics can be derived from the *exact* solution cost of a *relaxed* version of the problem

If the rules of the 8-puzzle are relaxed so that a tile can move anywhere, then  $h_1(n)$  gives the shortest solution

If the rules are relaxed so that a tile can move to any adjacent square, then  $h_2(n)$  gives the shortest solution

Key point: the optimal solution cost of a relaxed problem is no greater than the optimal solution cost of the real problem

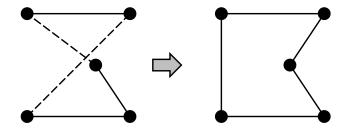
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### Example: Travelling Salesperson Problem

Find the shortest tour that visits each city exactly once



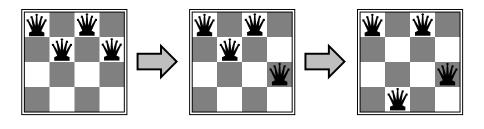
Minimum spanning tree heuristic can be computed in  $O(n^2)$ and is a lower bound on the shortest (open) tour.







# Put *n* queens on an $n \times n$ board with no two queens on the same row, column, or diagonal









### Hill-climbing (or gradient ascent/descent)

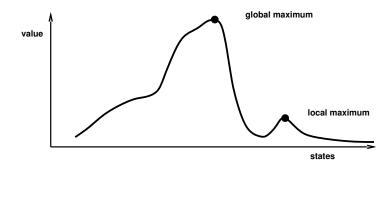
"Like climbing Everest in thick fog with amnesia"

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Problem: depending on initial state, can get stuck on local maxima

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### Simulated annealing

Idea: escape local maxima by allowing some "bad" moves but gradually decrease their size and frequency

```
function Simulated-Annealing( problem, schedule) returns a solution state
      inputs: problem, a problem
               schedule, a mapping from time to "temperature"
      local variables: current, a node
                         next. a node
                         T, a "temperature" controlling the probability of downward
  steps
      current \leftarrow Make-Node(Initial-State[problem])
      for t \leftarrow 1 to \infty do
            T \leftarrow schedule[t]
            if T=0 then return current
            next \leftarrow a randomly selected successor of current
            \Delta E \leftarrow Value[next] - Value[current]
            if \Delta E > 0 then current \leftarrow next
            else current \leftarrow next only with probability e^{\Delta E/T}
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                                                                                              Organizational
```





### Properties of simulated annealing

At fixed "temperature" T, state occupation probability reaches Boltzman distribution:

$$p(x) = \alpha e^{\frac{E(x)}{kT}}$$

 $\mathcal{T}$  decreased slowly enough  $\implies$  always reach best state.

Is this necessarily an interesting guarantee?

Devised by Metropolis et al., 1953, for physical process modelling Widely used in VLSI layout, airline scheduling, etc.







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• MIT online course on AI (available for free):

https://ocw.mit.edu/courses/electrical-engineering-and-computer-science/6-034-artificial-intelligence-scienc

• Original version of these slides used at Berkeley by Russel in his Al course, based on the Al book of Norvig and Russel:

http://aima.eecs.berkeley.edu/slides-pdf/

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- Assignment code: REPO/assignment\_6/src/\*.lisp
- Assignment points: 7 points
- Assignment due: 28.11, Wednesday, 23:59 AM German time
- Next class: 29.11, 14:15
- Next class topic: introduction to ROS. (Make sure your ROS and roslisp\_repl are working.)





### Thanks for your attention!

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